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Automatic Music Composition using Answer Set Programming

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Abstract
Music composition used to be a pen and paper activity. These these days music is often composed with the aid of computer software, even to the point where the computer compose parts of the score autonomously.

The composition of most styles of music is governed by rules. We show that by approaching the automation, analysis and verification of composition as a knowledge representation task and formalising these rules in a suitable logical language, powerful and expressive intelligent composition tools can be easily built.

This application paper describes the use of answer set programming to construct an automated system, named ANTON, that can compose melodic, harmonic and rhythmic music, diagnose errors in human compositions and serve as a computer-aided composition tool. The combination of harmonic, rhythmic and melodic composition in a single framework makes ANTON unique in the growing area of algorithmic composition.

With near real-time composition, ANTON reaches the point where it can not only be used as a component in an interactive composition tool but also has the potential for live performances and concerts or automatically generated background music in a variety of applications. With the use of a fully declarative language and an “off-the-shelf” reasoning engine, ANTON provides the human composer a tool which is significantly simpler, more compact and more versatile than other existing systems.

KEYWORDS: Answer set programming, applications of ASP, music composition, algorithmic composition, harmonic and melodic composition, diagnosis

1 Introduction
Music, although it seeks to communicate via emotions, is almost always governed by complex and rigorous rules which provide a foundation on which artistic expression can be based. In the case of musical composition, in most styles there are rules
which describe the progression of a melody, both at the local level (the choice of
the next note) and at the global level (the overall structure). Other rules describe
the harmony, which arises from the relationship between the melodic line and the
supporting instruments. A third set of rules determines the rhythm, the intervals
between notes, of a piece.

These rules were developed to guide and support human composers working in
the style of their choice, but we wish to demonstrate here that by using knowledge
representation techniques, we can create a computer system that can reason about
and apply compositional rules. Such a system will provide a simple and flexible
way of composing music automatically. Provided that the representation technology
used is sufficiently flexible to allow changes at the level of the rules themselves, the
system will also help the human composer to understand, explore and extend the
rules (s)he is working with.

Since the beginning of recorded time, music composers have used a number of
processes to generate the next note, be it simple scales or arpeggios, or complex
mathematical structures. The interest in developing computational systems for com-
posing, harmonising and accompanying music is not new either. Researchers have
used a variety of mechanisms in searching for a viable system, including encodings
of the stochastic and symbolic music of Xenakis (1992), and attempts to find sim-
pler schemes to the major work in artificial intelligence on the harmonisation of
Bach chorales by Ebcio˘glu (1986).

This paper describes Anton, an automatic composition system capable of simple
melodies with accompaniment, in particular for species one counterpoint as prac-
tised in the early Renaissance. The insights gained from this system can be and are
being extended to other musical styles, by adding or changing the rules. What has
impressed us has been particularly the ease in which musical experience could be
converted into code which is succinct and easy to verify.

Anton uses Answer Set Programming (ASP) (Gelfond and Lifschitz 1988), a
logic programming paradigm, to represent the music knowledge and rules of the
system. A detailed description is provided in Section 3, after a short description of
the musical aspects of the project (Section 2).

The initial system, Anton v.1.0, was first presented in (Boenn et al. 2008). In this
paper, we present Anton v.1.5. The simplicity of the basic encoding is presented in
Section 4. As we will demonstrate, the new version excluding rhythm is significantly
faster allowing Anton to be used in real-time application rather than just as an
interactive tool.

The initial system (Boenn et al. 2008), has only an extremely simple concept of
rhythm, all notes having the same length. In Section 5 we show how this musical
restriction has been relaxed, allowing interesting and “correct” rhythmic patterns.
The paper is completed with a discussion of the performance, both musical and
computational in Section 6, the use of ASP in Section 7 and future work in Section 8.

Our overall aim is multi-faceted; on the one hand we want develop musicological
ideas, create music, and test musical thoughts and on the other can use the system
to test the quality and utility of ASP solvers in real-world applications\(^1\). We also note that Anton is usable as part of a student marking system, checking that harmonisations fit the rules. Alternatively, the system can be used as a diagnostic and assisted composition tool, where a part of the piece is given to the program to be correctly completed.

2 Music Theory

Music is a world-wide phenomenon across all cultures. The details of what constitutes music may vary from nation to nation, but it is clear that music is an important component of being human.

In the work of this paper we are concentrating on western traditional tonal musics, but the underlying concepts can be translated to other traditions. The particular area of interest here is composition; that is creating new musical pieces.

Creating melodies, that is sequences of pitched sounds, is not as easy as it sounds. We have cultural preferences for certain sequences of notes and preferences dictated by the biology of how we hear. This may be viewed as an artistic (and hence not scientific) issue, but most of us would be quick to challenge the musicality of a composition created purely by random whim. Students are taught rules of thumb to ensure that their works do not run counter to cultural norms and also fit the algorithmically definable rules of pleasing harmony when sounds are played together.

“Western tonal” simply refers to what most people in the West think of as “classical music”, the congenial Bach through Brahms, music which feels comfortable to the modern western ear because of its adherence to familiar rules. Students of composition in conservatoires are taught to write this sort of music as basic training. They learn to write melodies and to harmonise given melodies in a number of sub-versions. If we concentrate on early music then the scheme often called informally “Palestrina Rules” is an obvious example to used for such a task. Similarly, harmonising Bach chorales is a common student exercise, and has been the subject of many computational investigations using a variety of methods.

For the start of this work we have opted to work with Renaissance Counterpoint. This style was used by composers like Josquin, Dufay or Palestrina and is very distinct from the Baroque Counterpoint used by composers like Bach, Haendel.

We have used the teaching at one conservatoire in Köln to provide the basic rules, which were then refined in line with the general style taught. The point about generating melodies is that the “tune” must be capable of being accompanied by one or more other lines of notes, to create a harmonious whole. The requirement for the tune to be capable of harmonisation is a constraint that turns a simple sequence (a monody) to a melody.

In this particular style of music complete pieces are not usually created in one

\(^1\) This paper is not intended to be a benchmarking paper for the various solvers and their numerous option. In this paper we simply wish to demonstrate that ASP is an appropriate paradigm for music composition and that composition can be done in near real-time.
go. Composers create a number of sections of melody, harmonising them as needed, and possibly in different ways, and then structuring the piece around these basic sections. Composing between 4 bars and 16 bars is not only a computationally convenient task, it is actually what the human composer would do, creating components from which the whole is constructed. So although the system described here may be limited in its melodic scope, it has the potential to become a useful tool across a range of sub-styles.

2.1 Automatic Composition

A common problem in musical composition can be summarised in the question “where is the next note coming from?”. For many composers over the years the answer has been to use some process to generate notes. It is clear that in many pieces from the Baroque period that simple note sequences are being elaborated in a fashion we would now call algorithmic. For this reason we can say that algorithmic composition is a subject that has been around for a very long time. It is usual to credit Mozart’s Musikalisches Würfelspiel (Musical Dice Game) (Chuang 1995) as the oldest classical algorithmic composition, although there is some doubt if the game form is really his. In essence the creator provides a selection of short sections, which are then assembled according to a few rules and the roll of a set of dice to form a Minuet\(^2\). Two dice are used to choose the 16 minuet measures from a set of 176, and another die selects the 16 trio measures\(^3\), this time from 96 possibilities. This gives a total number of \(1.3 \times 10^{29}\) possible pieces. This system however, while using some rules, relies on the coherence of the individual measures. It remains a fun activity, and recently web pages have appeared that allow users to create their own original(ish) “Mozart” compositions\(^4\).

In the music of the second Viennese school (“12-tone”, serial music) there is a process of action, rotating, inverting and use of retrograde, but usually this is performed by hand.

More recent algorithmic composition systems have concentrated on the generation of monody\(^5\), either from a mathematical sequence, chaotic processes, or Markov chains, trained by consideration of acceptable other works. Frequently the systems rely on a human to select which monodies should be admitted, based on judgement rather than rules. Great works have been created this way, in the hands of great talents. Probably the best known of the Markov chain approach is Cope (2006)’s significant corpus of Mozart pastiche.

In another variation on this approach, the accompanist, either knowing the chord structure and style in advance, or using machine-listening techniques, infers a style

\(^2\) A dance form in triple time, \textit{i.e.} with 3 beats in each measure  
\(^3\) A Trio is a short contrasting section played before the minuet is repeated  
\(^4\) For example http://www.softsynth.com/jasyn/examples/dicegame/  
\(^5\) A monody is a single solo line, in opposition to homophony and polyphony
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of accompaniment. The former of these approaches can be found in commercial products, and the latter has been used by some jazz performers to great effect, for example by George E. Lewis (2000).

A more recent trend is to cast the problem as one of constraint satisfaction. For example PWConstraints is an extension for IRCAM’s Patchwork, a Common-Lisp-based graphical programming system for composition. It uses a custom constraint solver employing backtracking over finite integer domains. OMSituation and OMCclouds are similar and are more recently developed for Patchwork’s successor OpenMusic. A detailed evaluation of them can be found in (Anders 2007), where the author gives an example of a 1st-species counterpoint (two voices, note against note) after (Fux 1725) developed with Strasheela, a constraint system for music built on the multi-paradigm language Oz. Our musical rules implement the melody and counterpoint rules described by (Thakar 1990), which we find give better musical results.

One can distinguish between improvisation systems and composition systems. In the former the note selection progresses through time, without detailed knowledge of what is to come. In practice this is informed either by knowing the chord progression or similar musical structures (Brothwell and fitch 2008), or using some machine listening. In this paper we are concerned with composition, so the process takes place out of time, and we can make decisions in any order.

It should also be noted that these algorithmic systems compose pieces of music of this style in either a melodic or a harmonic fashion, and are frequently associated with computer-based synthesis. The system we will propose later in this paper is unique as it deals with both simultaneously.

2.1.1 Melodic Composition

In melodic generation a common approach is the use of some kind of probabilistic finite state automaton or an equivalent scheme, which is either designed by hand (some based on chaotic oscillators or some other stream of numbers) or built via some kind of learning process. Various Markov models are commonly used, but there have been applications of n-grams, genetic algorithms and neural nets. What these methods have in common is that there is no guarantee that melodic fragments generated have acceptable harmonisations. Our approach, described below is fundamentally different in this respect, as our rules cover both aspects simultaneously.

In contrast to earlier methods, which rely on learning, and which are capable of giving only local temporal structure, a common criticism of algorithmic melody (Leach 1999), we do not rely on learning and hence we can aspire to a more global, whole melody, approach. Furthermore, learning is designed to work in one direction at the time which makes it hard to use in a partially automated fashion. Our systems is not bound to these limitation, so operations like “fill in the 4 notes between these sections” are not a problem for us.

Researchers are also trying to move beyond experiments with random note generation because the results are too lacking in structure. Predictably, the alternative of removing the non-determinism at the design stage (or replacing with a proba-
bilistic choice) runs the risk of ‘sounding predictable’! There have been examples of good or acceptable melodies created like this, but the restriction inherent in the process means it probably works best in the hands of geniuses.

Our experience with this work made us realise how many acceptable melodies can be created with only a few rules, and as we add rules, how much better the musical results are.

### 2.1.2 Harmonic Composition

A common usage of algorithmic composition is to add harmonic lines to a melody; that is notes played at the same time as the melody that are in general consonant and pleasing. This is exemplified in the harmonisation of 4-part chorales, and has been the subject of a number of essays in rule-based or Markov-chain systems. Perhaps a pinnacle of this work is Ebcioğlu (1986) who used early expert system technology to harmonise in the style of Bach, and was very successful. Subsequently there have been many other systems, with a range of technologies. A review of these is included in (Rohrmeier 2006).

Clearly harmonisation is a good match to constraint programming based systems, there being accepted rules\(^6\). It also has a history from musical education.

But these systems all start with a melody for which at least one valid harmonisation exists, and the program attempts to find one, which is clearly soluble. This differs significantly from our system, as we generate the melody and harmonisation together, the requirement for harmonisation affecting the melody.

### 3 Answer Set Programming

*Answer Set Programming* (Baral 2003; Gelfond and Lifschitz 1988) is a declarative programming paradigm in which a logic program is used to describe the requirements that must be fulfilled by the solutions of a certain problem. The answer sets of the program, usually defined through (a variant/extension of) the stable model semantics (Gelfond and Lifschitz 1988), are interpreted to the solutions of the problem. This technique has been successfully applied in domains such as planning (Eiter et al. 2002; Lifschitz 2002), configuration and verification (Soininen and Niemelä 1999), super-optimisation (Brain et al. 2006), diagnosis (Eiter et al. 1999), game theory (De Vos and Vermeir 1999) multi-agent systems (Baral and Gelfond 2000; Buccafurri and Gottlob 2002; De Vos and Vermeir 2004; Buccafurri and Caminiti 2005; Cliffe et al. 2006), reasoning about biological networks (Grell et al. 2006), voting theory (Konczak 2006), policy mechanisms (Mileo and Schaub 2006), generation of phylogenetic trees (Erdem et al. 2006), evolution of language (Erdem et al. 2003) and game character descriptions (Padovani and Provetti 2004).

There is a large body of literature on ASP: for in-depth coverage see (Baral 2003), but for the sake of making this paper self-contained we will cover the essentials as they pertain to our usage here.

Basic Concepts: The answer set semantics is a model based semantics for normal logic programs. Following the notation of (Baral 2003), we refer to the language of normal logic programs under the answer set semantics as AnsProlog.

The smallest building block of an AnsProlog program is an atom or predicate, e.g. r(X,Y) denotes XrY. e.g owns(X,Y) stating that X owns Y. X and Y are variables which can be grounded with constants, e.g. owns(alice,key). Each ground atom can be assigned the truth value true or false.

In this paper we will only consider programs with one type of negation, namely negation-as-failure denoted not. This type of negation states that something should be assumed false when it cannot be proven to be true. A literal is an atom a or its negation not a, with not not a = a. We extend the notation to sets: not S is the set \{not l | l ∈ S\} with S a set of literals.

An AnsProlog program consist of a finite set of statements, called rules. Each rule \( r : a ← B \) or \( ⊥ ← B \) is made of two parts namely the body B, denoted \( B_r \), which is a set of literals, and a head atom a or ⊥, denoted \( H_r \). The body can be divided in two parts: the set of positive atoms, denoted as \( B^+_r \), and the set of negated atoms, denoted \( B^-_r \). A rule should be read as: “a is supported if all elements of B are true”. A rule with empty body is called a fact and we often only mention the head. A rule with head ⊥ is referred to as an (integrity) constraint. We often omit the ⊥ symbol and leave the head empty. ⊥ is always assigned the truth value “false”. A program is called positive if it does not contain any negated literals.

The finite set of all constants that appear in the program \( P \) is referred to as the Herbrand Universe, denoted \( U_P \). Using the Herbrand universe, we can ground the entire program. Each rule is replaced by its ground instances, which can be obtained by replacing each variable symbol by an element of \( U_P \). The ground program, denoted ground(\( P \)), is the union of all ground instances of the rules in \( P \).

The set of all atoms grounded over the Herbrand universe of a program is called the Herbrand Base, denoted as \( \mathcal{B}_P \). These are exactly those atoms that will appear in the ground program.

An assignment of truth values to all atoms in the program (or all elements from the Herbrand base) is called an interpretation. Often only those literals that are considered true are mentioned, as all the others are false by definition (negation as failure).

Given a ground rule \( r \), we say a \( r \) is applicable w.r.t. an interpretation \( I \subseteq \mathcal{B}_P \) if all the body elements are true \((B^+_r \subseteq I \text{ and } B^-_r \cap I = \emptyset)\). The rule is applied w.r.t. \( I \) when it is applicable and \( H_r \in I \). A ground rule is satisfied w.r.t. an interpretation \( I \) if it is either not applicable or applied w.r.t. \( I \). An atom is supported w.r.t. \( I \) if there is an applied rule with this atom in the head. Obviously, we want to make sure that interpretations satisfy every rule in the program. So, an interpretation \( I \) is a model for a program \( P \) if and only if all rules in ground(\( P \)) are satisfied.

To find actual solutions, models alone are not sufficient: we need to make sure that only those literals that are supported are considered true. This results in the so-called minimal model semantics. A model \( M \) for a program \( P \) is minimal if no other model \( N \) exists such that \( N \subset M \). Programs can have any number of minimal models, while programs without constraints will always admit at least one. Positive
programs will have at most one minimal model, and exactly one when they do not admit any constraints.

The minimal model of a positive program without constraints can be found using a fixpoint, called the deductive closure, which can be computed in polynomial time. We start with the empty set and find all atoms that are supported. With this new set we continue to find supported atoms. When the set reaches a fixpoint, we have found the deductive closure or minimal model of the program. When the program contains constraints, we can follow the same principle but the process fails when a unsatisfied constraint is found.

**Definition 1**
Let $P$ be a positive AnsProlog program and let $I$ be an interpretation. We define the immediate consequence operator $T_P$ as:

$$T_P(I) = \{ a \in B_P \mid \exists r \in P : B_r \subseteq I \}$$

$T_P$ is monotonic so it has a least fixpoint, denoted $T_P^\omega(\emptyset)$, which corresponds to the deductive closure.

**Definition 2**
Let $P$ be a positive AnsProlog program. The deductive closure of $P$, is the least fixpoint $T_P^\omega(\emptyset)$ of $T_P$.

The minimal semantics is sufficient for positive programs, but fails in the presence of negation-as-failure. A simple example of such a program is: \{ $a \leftarrow \text{not } a$ ; $b \leftarrow a$ \}. This program has one minimal model \{ $a, b$ \}, while the truth of $a$ depends on $a$ being false. To obtain intuitive solutions, we need to verify that our assumptions are indeed correct. This is done by reducing the program to a simpler program containing no negation-as-failure. Given an interpretation, all rules that contain $\text{not } l$ that are considered false are removed while the remaining rules only retain their body atoms. This reduction is often referred to as the Gelfond-Lifschitz transformation (Gelfond and Lifschitz 1988; Gelfond and Lifschitz 1991). When this program gives the same supported literals as the ones with which we began, we have found an answer set.

**Definition 3**
Let $P$ be a ground AnsProlog program. The Gelfond-Lifschitz transformation of $P$ w.r.t a set of ground atoms $S$, is the program $P^S$ containing the rules $H_r \leftarrow B_r^+$ such that $H_r \leftarrow B_r^+$, $\text{not } B_r^- \in P$ with $B_r^- \cap S = \emptyset$.

**Definition 4**
Let $P$ be an AnsProlog. A set of ground atoms $S \subseteq B_P$ is an answer set of $P$ iff $S$ is the minimal model of $\text{ground}(P^S)$.

The non-deterministic nature of negation-as-failure gives rise to several answer sets, which are all acceptable solutions to the problem that has been modelled. It is in this non-determinism that the strength of answer set programming lies.
Extensions The basic language, single head atom and negation-as-failure only appearing in the body, already enables the representation of many problems. However, for some applications the programmer is forced to write code in a more round-about non-intuitive way. To overcome this, several extensions were introduced.

For this paper we use one of these extensions: choice rules (Niemelä et al. 1999). A lot of problems require choices to made between a set of atoms. Although this can be modelled in the basic formalism it tends choice rules are offer more clarity of expression and are more convenient. Choice rules, written $L\{l_1, \ldots, l_n\} M$, are a convenient construct to state that at least $L$ and at most $M$ from the set $\{l_1, \ldots, l_n\}$ must be true in order to satisfy the construct. $L$ defaults to 0 when omitted while $M$ defaults to $n$. Choice rules are often used in conjunction with a grounding predicate: $L\{A(X) : B(X)\} M$ represents the choice of a number of atoms $A(X)$ where is grounded with all values of $X$ for which $B(X)$ is true.

Implementations: Algorithms and implementations for obtaining answer sets of logic programs are referred to as answer set solvers. The most popular and widely used solvers are smodels (Niemelä and Simons 1997) and dlv (Eiter et al. 1998) and more recently clasp (Gebser et al. 2007a).

Alternatives are cmodels (Giunchiglia et al. 2004) and sup (Lierler 2008), solvers based on translating the program to a SAT problem, and smodels-ie (Brain et al. 2007), the cache-efficient version of smodels. Furthermore, there is the distributed solver Platypus (Gresse & al. 2005).

To solve a problem it first needs to be grounded. Currently three grounders are used: the grounder integrated with dlv, lparse, the grounder that was developed together with smodels but is used by most solvers, and the most recent one Gringo (Gebser et al. 2007) which works together with clasp and other solvers that take lparse output. During the grounding phase, not only are the variables substituted for constants, but also useless rules are eliminated. Furthermore, grounders try to simplify the program as much as possible. The second phase is solving which takes a grounded program or its internal representation as input and generates the set of its answer sets.

Current answer set solvers can be divided in three groups depending on the style of algorithm they use or the mapping the use: depth first search (DPLL) clause learning and a mapping to SAT. All use a variety of heuristics to improve the performance of the basic algorithm.

4 Anton

4.1 System Description

ANTON is an algorithmic composition system that uses ASP techniques to represent and reason about compositional rules. Aprolog is used to write a description of the rules that govern the melodic and harmonic properties of a correct piece of music; in this way the program describes a model of musical composition that can be used to assist the composer by suggesting, completing and verifying short pieces.
The composition rules are modelled so that the AnsProlog program defines the requirements for a piece to be musically valid, and thus every answer set corresponds to a different valid piece. To generate a new piece the composition system simply has to generate an (arbitrary) answer set.

In this section we will discuss the basic system of Anton v.1.5. The handling of rhythm will be discussed in Section 5 page 15.

The AnsProlog program of the basic system is created from various files: notes.lp, modes.lp, progression.lp, melody.lp, harmony.lp and chord.lp. The first contains the general background rules on notes and intervals while the second describes the various modes/keys the system can use and their consequences for note selection and position. The current system is able to work with major, minor, Dorian, Lydian and Phrygian modes. Rules for the progression of all parts, either melodic and harmonic, are handled in progression.lp. This part of the program is responsible for selecting the next note in each of the parts on the basis of the previous note. The rules for the melodic parts and for composing with multiple parts are encoded in melodic.lp and harmonic.lp respectively. chord.lp provides the description of chords and chordal progression and the effects of note choices.

We will discuss progression, melody and harmony in more detail. The whole system is licensed under the GPL and publicly available.7

Figure 1 presents a selection of rules dealing with the progression of notes. The

7 The source code is available from http://www.cs.bath.ac.uk/~mjb/anton/
model is defined over a number of time steps, given by the variable T. The key proposition is \texttt{chosenNote(P,T,N)} which represents the concept “At time T, part P plays note N”. To encode the options for melodic progress (“the tune either steps up or down one note in the key, leaps more than one note, repeats or rests”), choice rules are used. For diagnostic and debugging purposes, compositional errors are not immediately encoded as constraints, but instead use error rules like \texttt{error(P,T,err_ip) :- incorrectProgression(P,T)}. By using a constraint to obtain answer sets with error-atoms or excluding them entirely, we can alter the functionality of our system from diagnosis to composition without changing the code. We will later return to various applications of our system.

To encode the melodic limits on the pattern of notes and the harmonic limits on which combinations of notes may be played at once, error-rules like the one in \texttt{progression.lp} are included. Figure 2 shows how we encoded rules that forbid repetition of notes in the melodic parts, octave leaps except for special circumstances, impulses, repetition of more than two notes and certain lengths of intervals. While some of these rules might be valid in other types of music, Renaissance counterpoint explicitly forbids them.

Interaction between parts is governed by the rules of harmony. Figure 3 shows how we encoded the musical rules that specify that you cannot have dissonant intervals between parts, that limit the distance between parts and that state that parts cannot cross-over.

While the fragments shown in Figures 1-3 are a subset of the knowledge base, they demonstrate that the rules are very simple and intuitive (with the necessary musical background). The modelling of this style of music, excluding rhythm, contains less than 400 ungrounded logic rules.
In the previous section we discussed the basic components of the ANTON system. However, in order to have a complete system, we are still missing one component: the specification of parts. Currently, the system comes with descriptions for solos, duets, trios and quartets but the basic system is written with no fixed number of parts in mind. Figure 4 shows the description for a quartet.

Depending on how the system is used, for composition or diagnosis, one will either be interested in those pieces that do not result in errors at all, or in an...
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Fig. 5. The score and human readable format for the tunes composition.

answer set that mentions the error messages. For the former we simply specify the constraint :- error(P,T,R), effectively making any error rule into a constraint. For the latter we include the rules: errorFound :- error(P,T,R), and :- not errorFound, requiring that an error is found (i.e. returning no answers if the diagnosed piece is error free). These simple rules are encoding in composing.lp and diagnosis.lp so that they can be included when our scripts assemble to program.

By adding constraints on which notes can be included, it is possible to specify a part or all of a melody, harmony or complete piece. This allows ANTON to be used for a number of other tasks beyond automatic composition. By fixing the melody it is possible to use it as an automatic harmonisation tool. By fixing part of a piece, it can be used as computer aided composition tool. By fixing a complete piece, it is possible to check its conformity with the rules, for marking student compositions or harmonisations. Alternatively we could request the system to complete part of a piece.

The complete system consists of three major phases; building the program, running the AnsProlog program and interpreting the results. As a simple example suppose we wish to create a 4 bar piece in E major. One would write:

```
programBuilder.pl --task=compose --mode=major --time=16 > program
```

which builds the AnsProlog program, giving the length and mode. Then

```
gringo < program | ./shuffle.pl 6298 | clasp 1 > tunes
```

runs the solving phase and generates a representation of the piece. We provide a number of output formats, one of which is a Csound (Boulanger 2000) program with a suitable selection of sound templates.

```
$ parse.pl --fundamental=e --output=csound < tunes > tunes.csd
```

generates the Csound input from the generic format, and then

```
$ csound tunes.csd -o dac
```

plays the melody. We provide in addition to Csound, output in human readable format, AnsProlog facts or the Lilypond score language. Figure 5 shows the score of the tunes piece composed above.

Alternatively we could request the system to complete part of a piece. In order to do so, we provide the system with a set of AnsProlog facts expressing the mode, the notes which are already fixed, the number of notes in your piece, the configuration and the number of parts.
Figure 6 contains an example of such file.

We then use the system as before with the exception of adding \texttt{--piece=musing.lp} when we run \texttt{programBuilder.pl}. The system can then return all possible valid composition that satisfy the criteria set out in the partial piece.

\textit{Anton} is not limited to the composition of music; it can also be used verifying whether a (partial) piece of music adheres to the rules of compositions. Take for example the composition in Figure 7. Using the command-line options \texttt{--task=diagnosis --piece=problems.lp} when we run \texttt{programBuilder.pl}, the system will return the error codes for all the rules that the composition breaks. In case of \texttt{problems.lp}, we obtain:

\begin{verbatim}
error(1,2,"Repeated pattern") error(1,4,"Repeated pattern") error(1,2,"Split melody")
\end{verbatim}

The first two errors indicate that we have repeated patterns: e.g. from the second note we leap up by a perfect fourth and step down by a major second. This pattern is then repeated starting at the fourth and sixth notes. The repeated progression pattern also triggers the split melody error. Split melodies occur when the even/odd notes form separate melodies.

The \textit{AnsProlog} programs used in \textit{Anton} v.1.5, contains just 509 lines (not including comments and empty lines) and encodes 44 melodic, harmonic and rhythmic rules. Once instantiated, the generated programs range from 1,000 atoms and 5,500 rules (a solo piece with 4 notes) to 22,000 atoms and 796,000 rules (a 32 note quartet). It should be noted that our 1500 lines of code, \textit{AnsProlog} rules and perl scripts combined, contrast with the 8000 lines in Strasheela (Anders 2007) and 88000 in Bol (Bel 1998).

The question of problem complexity is still open. Clearly there is an NP algorithm for generating a piece that meets a set of musical rules and there is no known polynomial algorithm for this task. Depending on what constitutes a valid musical style, it is likely that the task can be shown to be NP-Complete. Verifying if a certain composition satisfies all the musical rules is linear. However from an applications standpoint, the exact complexity of the process is of less importance than the run time performance.

\begin{verbatim}
keyMode(lydian).
chosenNote(1,1,25).
chosenNote(1,2,24).
chosenNote(1,8,19).
chosenNote(1,9,20).
chosenNote(1,10,24).
chosenNote(1,14,29).
chosenNote(1,15,27).
chosenNote(1,16,25).
#const t=16.
style(solo).
part(1).
\end{verbatim}

\textbf{Fig. 6.} \texttt{musing.lp}: An example of a partial piece
Our system used to be limited in terms of one of the most essential musical parameters: rhythm. All music ANTON v.1.0 generated was based on rules for classical polyphony, *i.e.* the combination of musically unique, independent melodic voices, but all events had the same time interval. Within this restriction we are able to generate first-species counterpoint up to four independent voices and solo melodies as well as homophonic 4-part chorales where the rules for the inner voices could be more relaxed from the strict melodic rules that determine each of the four voices in a polyphonic setting.

Rhythm determines at what point in time a particular note in a sequence is played, for how long it is played and how much stress this note will get. The musical experience is partly determined by the constant inter-change of *impact* and *resolution*. Both influence the behaviour of musical parameters on micro- and macro-structural levels and are expressed within the rhythm of the piece.

An alternative characterisation of rhythm is as the interplay between the duration of notes. The relation between notes can then be expressed in terms of interval relationships Allen (1983). Thus temporal interval logic Goranko et al. (2003) style reasoning can be used to describe a constructive model of rhythm. Our experience has shown that access to the full range of interval relations is unnecessary and difficult to encode, thus ANTON uses a simpler mechanism, that collects many of the relationships into one “overlaps” literal. This is sufficient for the rhythms of our musical genre and it is this simpler form that we describe here.

Our representation of rhythm is closely related to Farey sequence. The Farey sequence of order n can defined as the sequence of reduced fractions in the range [0,1], when in lowest terms, have denominators less than or equal to n, arranged in order of increasing size. The \( n^{th} \) term in the sequence is the set of rational numbers
with \( n \) as denominator. An example the sequence of order 8 is
\[
F_8 = \frac{0}{1}, \frac{1}{8}, \frac{1}{7}, \frac{2}{6}, \frac{3}{5}, \frac{3}{4}, \frac{4}{3}, \frac{5}{2}, \frac{5}{1}
\]
The related concept we will use is the filtered Farey sequence, which is a systematic filtering of this sequence. In particular we will show how it is used in the description of rhythm in the next subsection, and indicate the constructive programming aspects in Section 5.2.

### 5.1 Musical Discussion of Rhythm

The musical areas of harmony and classical counterpoint often have rules about the conditions when a particular constellation of notes may occur on the timeline, sometimes with inclusion of the events preceding and following. For example, a **suspended fourth** is a dissonant constellation of two or more voices created on a strong beat. The voice that suspends the consonant note, i.e., the fourth note of the scale suspending the third, needs to be sounding before the dissonance occurs. This sound needs also to be consonant. After the dissonance on the strong beat the suspending voice needs then to resolve on a weak time interval within the measure. That sound again must be a consonance. To help expressing such rules the interval relations of ‘start’, ‘end’, ‘during’ and ‘overlap’ are needed. In music, however, the time intervals themselves are never ‘neutral’. There are typical alternations of strong and weak beats in nearly every musical style that is based on an underlying pulse. Those alternating beat patterns form the notion of meter. But, the concept of meter in Renaissance style is a particular one and not the same as the concept of bars, beats and time signatures that is prevailing since the Baroque era and which is still in use today.

There are generally four different kinds of musical time in the Renaissance. When looking at the subdivision of the brevis, which translates into today’s double whole-note, there are four different options for the composer of that area, as documented in the famous treatise ‘Ars Nova’ by Philippe de Vitry. The brevis can be interpreted either as 3 or 2 semi-breves (today’s whole note) and those further into 3 and 2 subdivisions called minims (today’s half note), so we can subdivide the longa into 3 x 2, 2 x 2, 3 x 3 or 2 x 3 minims\(^8\). Those different subdivisions were indicated in the vocal score using different time-signatures\(^9\). The 15th century composer Johannes Ockeghem wrote his *Missa prolationem*, a four-voiced polyphonic masterpiece, using all four different time-signatures together, a different one for each voice, while at the same time the voices imitate their lines containing the same melodic material using canons and double-canons\(^10\). This complex polyrhythmic structure

\(^8\) The order of subdivision is musically important in terms of accentuation and therefore has consequences for the treatment of consonance and dissonance. Hence, 3 x 2 is not the same as 2 x 3.

\(^9\) The four time signatures are called *tempus perfectum cum prolationem imperfecta* (3 x 2), *tempus imperfectum cum prolationem imperfecta* (2 x 2), *tempus perfectum cum prolationem perfecta* (3 x 3) and *tempus imperfectum cum prolationem perfecta* (2 x 3).

\(^10\) A canon is a special case of a line that can be imitated simultaneously by another voice \( n \) beats
Music Composition using ASP

‘X’ marks a downbeat, ‘O’ marks a 2nd level beat, ‘o’ marks a 3rd level beat

<table>
<thead>
<tr>
<th></th>
<th>X</th>
<th>O</th>
<th>O</th>
<th>O</th>
<th>X</th>
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<th>O</th>
<th>O</th>
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<td>X</td>
<td>O</td>
<td>O</td>
<td>O</td>
<td>O</td>
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Table 1. Polyrhythmic structure of downbeats from Ockeghem’s Missa prolationem creating a hyper-meter of 36 beats

<table>
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<tbody>
<tr>
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<td>O</td>
<td>O</td>
<td>O</td>
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<td>O</td>
<td>X</td>
</tr>
<tr>
<td>B</td>
<td>X</td>
<td>O</td>
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<td>O</td>
<td>O</td>
<td>O</td>
<td>X</td>
<td>O</td>
<td>O</td>
<td>O</td>
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<td>O</td>
<td>O</td>
<td>O</td>
<td>O</td>
<td>O</td>
<td>X</td>
</tr>
</tbody>
</table>

Table 2. Metrical hierarchy from Ockeghem’s Missa prolationem expressed as $F'_{36}$

establishes a proportion of note durations as 6:4:9:6 between the voices. The effect of superimposing different beat qualities can be seen in Table 1. Only the smaller note durations below the minim are not affected by the proportional scaling. They remain at the same length for all four voices regardless of their time-signature. When transcribed nowadays into common practice notation the voices would need 36 half notes to complete one large cycle of accent patterns before starting over with a common ‘downbeat’ (de la Motte 1981). The complete cycle therefore translates into the filtered Farey Sequence $F'_{36}$, where each of the ratios in the range of $[0...1]$ denotes the onset time of a half note; see the representation for one voice, the Bass, in Table 2. According to the time-signature (3 x 2) of that particular voice there are three distinct metrical layers that govern the note events occurring on such a grid: The top layer gives us the occurrence of the downbeat, which is the event of most metrical importance, i.e. no dissonance may occur here unless the voice causing it prepares the note on the preceding beat. The second layer denotes the beat level. Although of less metrical weight, no dissonant interval should sound here unless it is a prepared suspension. The third layer provides the lightest metrical events. Here dissonances may occur, for instance in form of a passing note. The rule demanding preparation of the dissonance is relaxed on this level and on all further subdivisions underneath.

The hierarchical pattern of one of Ockeghem’s voices in Table 2 shows also some later while their combination at the same time satisfies the rules on consonance/dissonance. Adding support for more sophisticated interval relations in future versions of ANTON will allow us to compose canons.
interesting properties that lead to a general method for the construction of such tables. Starting with the first metrical level (I) in Table 2, we see that the largest denominator is always equal to the number of measures required to come back to square one with all the other voices, i.e. the number of measures per hyper-meter. All the other denominators on level I are divisors of the largest denominator. The next level (II) shows us how many subdivisions are contained in the hyper-meter on that particular level. This is again indicated by the largest denominator of the level and all other denominators are his divisors excluding those already contained on all lower indexed levels. This principle repeats itself on all higher indexed metrical levels. For each denominator \( n \) in the scheme, the numerators also follow a simple principle: they traverse the complete ordered list of numbers co-prime to \( n \).

As we have shown in Boenn (2007) and Boenn (2008), the Farey Sequence is ideal for tasks like rhythmic modelling, music performance analysis and music theory. Chapter 3 of Hardy and Wright (1938) gives a description and proves the properties of the Farey Sequence. Its scalability and general independence from the concepts of bars and meter is of advantage because it can be applied to numerous different musical styles. We have given a glimpse in the above Renaissance example (Table 2) how it could be used to encode polyrhythmic structures. Other examples can include African Polyrhythm, Western Classical, Avantgarde and Popular Music, Greek Verse Rhythms, Indian Percussion and many more. The principle remains always the same.

The visualisation in Figure 8 clearly points out that the smaller the denominator the larger are the symmetrical gaps around the x-position of the ratio, i.e. the smaller \( b \) of the ratio \( a/b \), the greater the distance. We believe that it is due to those relatively large gaps surrounding simpler ratios that they form perceptually useful zones of attraction for more complex ratios that fall into them or that come close enough. It is left for future field studies to measure and to find evidence whether these zones of attraction are perceptually relevant or not. Composers who want to “stay away” from those simple ratios will need to leave a considerable amount of space around these zones of attraction. It becomes also clear that there are various accelerandi and ritardandi encoded in every \( F_n \), for example there are gestalts\(^{11}\) that form visible triangles between larger reciprocals and smaller ones in their surrounding area (Figure 8). These gestalts are formed by monotonically increasing or decreasing values of the denominators. The increasing or decreasing tendencies overlap each other. The gaps between the ratios forming those triangles are always on a logarithmic scale, hence the impression of accelerated or reduced tempo that becomes evident through the sonification of these triangular gestalts. It is well known that timed durations need to be placed on a logarithmic rather than linear scale in order to convey a “natural” sense of spacing and tempo modification. These structures are clearly mirrored around the 1/2 value that is part of every \( F_n \) with \( n > 1 \).

The great variety of styles and concepts from medieval to modern eras can be

\(^{11}\) That is the concept of shape or configuration of a whole perceived object.
realised by applying intelligent filtering methods to sieve through the sequences. Examples for filtering include probabilistic methods and filters exploiting the prime number composition of integers and ratios, for example b-smooth numbers, or Clarence Barlow’s function for the ‘Indigestibility’ of a natural integer (Hajdu 1993). The Farey Sequence has been known for a while in the area of musical tuning systems\textsuperscript{12}. Its use for rhythmic modelling has not been fully exploited yet; \textsc{Anton} is the first music application for composition where rhythms and musical forms will be generated on the basis of the principles outlined in this paper. The Farey Sequence $F_n$ is per se highly symmetrical and unfolds harmonic subdivisions of unity via a recursive calculation of mediant fractions\textsuperscript{13}. Every music that depends on an underlying beat or pulsation can be represented by using $F_n$ to denote the normalised occurrence of musical events, e.g. note onsets.

Off-Beat rhythms are extremely useful for generative purposes. Two or more of these rhythms stacked in layers can always generate new combinations by using different accentuation patterns and different dynamic processes. Again, the Farey-Sequence proves to be a very useful structure to realise this concept. The details are beyond what is necessary in this paper, but in Boenn (2009) it is shown that many styles like Bebop, Funk and 20th century Avantgarde, are modelled by this mechanism. Speech rhythm, as used in various musical styles are also within the scope.

Finally, Sima Arom’s study (Arom 1991) on African Polyrhythms has been very

\textsuperscript{12} For example Erv Wilson’s annotations of tunings used by Partch (1979) http://www.anaphoria.com/wilson.html
\textsuperscript{13} See http://mathworld.wolfram.com/FareySequence.html
influential on contemporary western composers because of his successful recording and transcription processes that form the basis of his further analysis. We are seeking to translate some of these principles into features for ANTON for creative purposes but also in order to proof the general use of our concept. But this is for the future (Section 8).

The main message is that the Farey sequence contains all that is necessary for a very wide range of rhythmic patterns. With an encoding of them in ansProlog we have all the infrastructure we need.

5.2 Rhythm in Anton

The question now arises how we can combine this generative model for rhythm with the rules for melody, counterpoint and harmony that have been already implemented in ANTON. Of central importance for musical experiences in our view is the constant inter-change of impact and resolution that influences the behaviour of musical parameters on micro- and macro-structural levels. One can compare impact with gathering musical energy (Thakar 1990) and resolution with the release of previously built-up energy. We were very careful to make sure that the melodic lines generated are following this principle. With the encoding of rhythm we have now the possibility to precisely control the timing aspect of when to turn the musical movement from impact to resolution.

Rhythm in ANTON v.1.5 is the first prototype and an improved version is under development. As mentioned earlier, the encoding of rhythm is based on the concept of Farey sequences. One can view each rational number in the sequence as a way of partitioning the range [0,1], and as any particular partitioning can be constructed from a series of partitioning by a rational number with a prime denominator, the full collection of possible rhythms can be considered as all possible trees of partitions. In the initial version we limit the partition denominators to be taken to be only the primes 2 and 3, which allows a sufficiently rich subset of trees (and hence rhythms) for our musical genre. The encoding allows other primes, at some computational cost.

While the Farey sequence is a useful form for traversing the rhythmic structure, the partitioning tree is a useful (computational) way of building up a filtered Farey sequence by using a top-down approach, starting with a section of time and working it down by way of making subdivisions. The filtering of the Farey sequence is then achieved through the constraint of allowing only small primes as subdividing numbers within the tree, i.e. 2 and 3 in our initial implementation of rhythm. The further advantage of having a tree is that it allows us to have an easy access to different metrical levels (measure, beat, notes), which is vital for the later addition of rules about impact/resolution and for rules governing usage of consonance/dissonance. An example of a partitioning tree can be found in Figure 10. Each part is divided in a number of measures, these forms the top layer of the tree (represented by rectangles in the example below). Each measure is then divided in a number of beats (diamond shapes), which control the emphasis of notes (the weight of shading). The
Each Farey tree has a given depth
\[ \text{depth}(F, M_D + B_D + D_D) := \text{measureDepth}(M_D), \text{beatDepth}(B_D), \text{durationDepth}(D_D). \]
level(1, DE) := \text{depth}(F, DE).

Each Farey tree is divided into three layers (top to bottom)
- Measure, beats and note duration
- (bars, time signature and note value)

\[ \text{measureLevel}(F, M_L) := \text{depth}(F, DE), \text{durationDepth}(D_D), \text{beatDepth}(B_D), \]
level(F, M_L) := DE - (D_D + B_D).

Map from nodes to time positions
- Mapping increments each time a node is present

\[ \text{nodeStep}(F, 0, 1) := \text{not present}(F, D_L, ND), \text{nodeStep}(F, ND-1, T), \]
\[ \text{nodeStep}(F, ND, T+1) := \text{not present}(F, D_L, ND), \text{nodeStep}(F, ND-1, T), \]
\[ \text{nodeStep}(F, ND, T+1) := \text{present}(F, D_L, ND), \text{durationLeafLevel}(F, D_L), ND > 0. \]

From this we derive a unique mapping from node to time step
\[ \text{timeToNode}(P, T, ND) := \text{present}(F, D_L, ND), \text{nodeStep}(F, ND-1, T-1), \]
\[ \text{nodeStep}(F, ND, T+1) := \text{present}(F, D_L, ND), \text{durationLeafLevel}(F, D_L), ND > 0. \]

Beat strength is created at the first level of the beat layer ...
\[ \text{nodeBeatStrength}(F, M_L+1, ND_2, 1) := \text{measureLeafLevel}(F, M_L), \text{node}(F, M_L, ND_1), \]
\[ \text{descendant}(F, D, M_L, ND_1, M_L+1, ND_2). \]

Lowest and highest notes must also be slower
\[ \text{playHighestNote}(P, T) := \text{chosenNote}(P, T, N), \text{lowestNote}(P, N). \]
\[ \text{playLowestNote}(P, T) := \text{chosenNote}(P, T, N), \text{lowestNote}(P, N). \]
\[ \text{timeStepDuration}(P, T, DS) := DS > 1. \]

Fig. 9. A small rhythm code fragment

Notes (circles) of the part are then grouped w.r.t. duration and placed within their respective beats. Individual notes are the leaves of the tree.

The current version, ANTON v.1.5, picks an arbitrary tree from a constrained set of possibilities and imposes it on the output, so all parts have the same rhythm. In future versions, melodic and harmonic changes will interact with the decision over which tree is chosen. The newest version, which is not yet released, extends this by adding rules to deal with beats, their strength, duration and the interplay between parts. These rules allow the parts to have independent, but related rhythms.

Figure 9 contains a small code fragment of the current rhythm section of the system. The fragments show a portion of the structure of the partition tree and its three layers of measures, beats and notes. Each of these layers have separate rules that govern them. The fragment also shows the mapping from notes to time instances. We have included the definition of beat strength and one of the constraints linking tone and speed.

While not shown in this code fragment, the rhythm code is, like the other sections, written in such a way that diagnosis is possible.

In order to include rhythm in a composition, it suffices to use the --rhythm option to the programBuilder.pl script. The command:

```
./programBuilder.pl --task=compose --mode=lydian --time=12 --style=duet --rhythm > rhythm-comp
```

composes a duet in Lydian with 12 notes per part.
The program can then be parsed using `parse.pl` to generate Csound, Lilypond and human readable output. Figure 10 shows the partitioning tree and the human score for the Lydian duet.

6 Evaluation

In this section we evaluate the performance of Anton both from a computational and a musical perspective. We mainly focus on the non-rhythm part of the released version 1.5 for stability and reproducibility.

6.1 Run-time Results

To evaluate the practicality of using answer set programming in a composition system we timed Anton v.1.5 without the rhythm version while composing a suite of score with increasing difficulty.

Tables 3-6 contains the timings for a number of answer set solvers (clasp (Gebser et al. 2007a), cmodels (Lierler and Maratea 2004), models (Syriänen and Niemelä 2001), models-ie (Brain et al. 2007), modelscc (Ward and Schlipf...
Music Composition using ASP

Table 3. "Time taken (in seconds) for a number of solvers generating a solo piece."

<table>
<thead>
<tr>
<th>Solvers</th>
<th>Length</th>
<th>Clasp 1.2.1</th>
<th>Cmodels 3.79</th>
<th>Smodels 2.33</th>
<th>Smodels-IE 1.0.0</th>
<th>Smodels-IE 1.0.0</th>
<th>Smodels-IE 1.0.0</th>
<th>Sup 0.4</th>
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</tr>
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</table>

Table 4. "Time taken (in seconds) for a number of solvers generating a duet piece."

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<th>Smodels 2.33</th>
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<td>31.63</td>
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</table>

Table 5. "Time taken (in seconds) for a number of solvers generating a trio piece."

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<tr>
<th>Solvers</th>
<th>Length</th>
<th>Clasp 1.2.1</th>
<th>Cmodels 3.79</th>
<th>Smodels 2.33</th>
<th>Smodels-IE 1.0.0</th>
<th>Smodels-IE 1.0.0</th>
<th>Smodels-IE 1.0.0</th>
<th>Sup 0.4</th>
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</table>

The results show a significant increase in performance from Anton v.1.0 reported in (Boenn et al. 2008). Then we were only able to compose duets up to length 16, which took 29.63 seconds using the fastest solver clasp. The current system, Anton v.1.5, only takes 1.01 seconds for the same composition using the same solver. Furthermore, we can now compose trios and quartets within a reasonable time frame.
<table>
<thead>
<tr>
<th>Length</th>
<th>Clasp 1.2.1</th>
<th>Cmodels 3.79</th>
<th>Smodels 2.33</th>
<th>SmodelsIE 1.0.0</th>
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<td></td>
<td></td>
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</tr>
</tbody>
</table>

Table 6. Time taken (in seconds) for a number of solvers generating a quartet piece.

While improvements in the underlying solvers are a factor in the steep increase in performance, they are not the main contributor. We obtained most of our increases by revisiting AnsProlog encoding and finding more compact representations. We have compacted the rule set of minor keys which gives some reduction in space and run time. We reformatted some of the harmony rules and relaxed them so they only apply to neighbouring parts rather than all parts. The removal of redundant constraints compacts the program by a surprising amount. The rewriting of the repeated notes section produced a massive increase in grounding while the improved encoding of highest and lowest note saved us about 150,000 grounded rules on 16 note duet and about 30% in run time. Ranges over two octaves is now only noted at the end of the program, rather than at the point at which it is triggered. While this is slightly less informative, it offers a more than significant speed-up.

These results show that the system, using the more powerful solvers, is not only fast enough to be used as a component in an interactive composition tool but, when restricting to shorter sequences, could be used for real-time generation of music.

It is also interesting to note that the only solvers able to generate longer sequences using two or more parts all implement clause learning strategies, suggesting that the problem is particularly susceptible to this kind of technique.

We have not included run-time results for the rhythm section. The implementation as this feature is still being explored and the results would not be representative.

6.2 Music Quality

The other way to evaluate the system is to judge the music it produces. This is a less certain process, involving personal values. However we feel that the music is acceptable, at least of the quality of some students of composition, and at times capable of moments of excitement. Pieces by ANTON v.1.0 have been played to a number of musicians, who apart from the rhythmic deficiency we are addressing have agreed that it is valid music. The introduction of rhythm is more recent, and consequently it has not been subjected to so much scrutiny. There are still some refinements that could improve the output but many of the short pieces are clearly valid, and musical. In figure 11 we present a short quartet sequence in the minor key, followed by four major key pieces composed using the ANTON system; the audio and score can be found in the same location as the other works.
The interested reader can find more examples on the web:
http://dream.cs.bath.ac.uk/anton

Fig. 11. Fragments by Anton

7 The Use of ASP in Anton

7.1 Why ASP?

While music appreciation is matter of personal taste, musicologists use sets of rules which determine to which style a musical composition belongs or whether a piece breaks or expands the common practice of a certain composer or era. These sets of rules also govern the composition. So an intuitive and obvious approach to automatic composition is to encode these rules and use a rule based algorithm to produce valid music compositions. This natural and simple way of encoding things is shown in terms of speed of development, roughly 2 man-months, sophistication of the results, the amount of code (about 500 lines of code) and flexibility; we
can not only easily encode different styles but the same application is usable not only for automated composition but also diagnosis and human assisted composition. Furthermore, we automatically gain from all improvements in the underlying solver.

7.2 Answer Set Synthesis

The conventional view of the ASP paradigm is in terms of problem solving. The problem is described using AnsProlog in such a way that the answer sets can be interpreted as the solutions to the problem. So the program provides the specification for a solution; the constraints that elements in the search space have to satisfy. For ANTON we use ASP for synthesis rather than problem solving. We are doing something subtly, but importantly different; we are using a solver to generate representative objects given a specification. This is more knowledge representation than problem solving, since the language is used to provide a computational description of the required object. We believe that this approach, Answer Set Synthesis opens new of possibilities for the use of AnsProlog as there are lots of applications for which we need parametrisable, consistent but not necessarily exceptional content. Take for example, the automatic generation of a virtual world: one specifies the components of the environment and their dependencies and the program will generate you the possible locations. Generation of test data and puzzles are just a few more examples.

7.3 ASP Methodology

In constructing ANTON a number of advantages of using answer set programming have become clear, as have a number of limitations.

Firstly, AnsProlog programs are very fast to write and very compact. As well as the obvious benefits, this means it is possible to develop the system at the same time as undertaking knowledge capture and to prototype features in the light of the advice of domain experts. Part of the reason why it is so fast to use is that rules are fully declarative. Programming thus focuses on expressing the concepts that are being modelled rather than having to worry about which order to put things in — such as which rules should come first, which concepts have higher priority, which choices should be made first, etc. This also makes incremental development easy as new constraints can be added one at a time, without having to consider how they affect the search strategy.

Being able to add rules incrementally during development turns out to be extremely useful (Brain et al. ) from a software engineering view point. During the development of ANTON, we experimented with a number of different development methodologies. As argued in (Cliffe et al. 2008), “visualisation” of answer sets is a very productive way bridging the gap between the problem domain and the program. For the musical application domain, the most effective approach was found to be first writing a script that translates answer sets to human readable score or output for a synthesiser. Next the choice rules were added to the program to create
all possible pieces, valid or not. Finally the constraints were incrementally added to restrict the output to only valid sequences. By building up a library of valid pieces it was possible to perform regression testing at each step and thus isolate bugs as soon as they were introduced.

Using answer set programming was not without issue. One persistent problem was the lack of mature development support tools, particularly debugging tools. SPOCK (Brain et al. 2007) was used but as its focus is on computing the reasons behind the error, rather than the interface issues of explaining these reasons to the user, it was normally quicker to find bugs by looking at the last changes made and which regression tests failed. Generally, the bugs that where encountered were due to subtle mismatches between the intended meaning of a rule and the declarative reading of the rule used. For example the predicate `stepUp(P,T)` is used to represent the proposition “At time T, part P steps up to give the note at time T+1”, however, it could easily be misinterpreted as “At time T-1, part P steps up to give the note at time T”. Which of these is used is not important, as long as the same declarative reading is used consistently for all rules. With the first “meaning” selected for ANTON, the rule:

```
chosenNote(1,T,N+S) :- chosenNote(P,T-1,N), stepUp(P,T), stepBy(P,T,S).
```

would not encode the intended progression of notes. Even for experienced programmers, maintaining consistency in the semantics of predicates can be hard. One possible way of supporting a programmer in avoiding these subtle errors would be to develop a system that translated rules into natural language, given the declarative reading of the propositions involved. It should then be relatively straightforward to check that the rule encoded what was intended.

8 Conclusions and Future Work

We have presented an algorithmic composition system that uses AnsProlog to describe rules captured from classical texts on first species counterpoint. The early system of Boenn et al. (2008) has been developed in two significant ways: greatly improved performance and the introduction of a coherent rhythm schema. However ANTON still has considerable scope for further development and enhancement.

The encoding of rhythm is still an area of active research. Although we now have a basic encoding of rhythm it still requires a lot of fine tuning. The use of Farey sequences and partitioning trees is the core of this. In Section 5 we already indicated that we intend to encode Sima Arom’s principles which he discovered when studying African Polyrhythms. The use of partitioning trees will need to be further developed to do so.

We have concentrated on first species counterpoint from an early time, but many of the rules apply to other styles. We have made a few experiments with rules for Bach chorales and for hymn tunes. We need to partition the current rule-sets into building blocks to facilitate reuse.

The current system can write short melodies effectively and efficiently. Devel-
Development work is still needed to take this to entire pieces. We can start from these melodic fragments but a longer piece needs a variety of different harmonisations for the same melody, and related melodies with the same harmonic structure and a number of similar techniques. We have not solved the difficult global structure problem but it does create a starting point on which we can build a system that is hierarchical over time scales; we have a mechanism for building syntactically correct sentences, but these need to be built into paragraph and chapters, as it were. It is not clear if this will be achieved within the current ASP system, or by a procedural layer built on top if it, or some other scheme.

To make the system more user-friendly, there is a need for a user interface, probably graphical, to select from the options and styles. We have avoided this so far, as the Musician-Machine Interface is a separate specialist area, but there are plans for such an interface to be designed in the next phase.

In real life pieces some of the rules are sometimes broken. This could be simulated by one of a number of extensions to answer set semantics (preferences, consistency restoring rules, defensible rules, etc.). However how to systematize the knowledge of when it is acceptable to break the rules and in which contexts it is ‘better’ to break them is an open problem.

For Anton we used AnsProlog as a computational description language rather than just a knowledge representation one. There is a tempting possibility to apply the same methodology and approach to other areas of content, such as maybe game map generation. Initial experiments show promise.

References


Brain, M., Cliffe, O., and De Vos, M. A pragmatic programmer’s guide to answer set programming. In *Proceedings of the 2nd Workshop of Software Engineering for Answer Set Programming (SEA’09)*, 49–63.


