Vacancy and Interstitial Oxide Ion Migration in Heavily Doped \( \text{La}_{2-x}\text{Sr}_x\text{CoO}_{4+\delta} \)

Cristina Tealdi, a,b Chiara Ferrara, b Piercarlo Mustarelli b and M. Saiful Islam c

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1. Introduction

Layered perovskite oxides belonging to the first member of the Ruddlesden-Popper series (\( \text{A}_n\text{B}_2\text{O}_{3n+1}; n=1 \)) and exhibiting the \( \text{K}_2\text{NiF}_4 \)-type structure are the subject of considerable interest as they display a variety of physical properties. These cover superconductivity, magnetoresistance, catalysis and mixed ionic-electronic conductivity. 1 The latter, in particular, has attracted recent attention for the possible application of \( \text{A}_2\text{BO}_4 \) compounds (\( \text{A}= \) rare earth; \( \text{B}= \) transition metal) as cathode materials in intermediate-temperature solid oxide fuel cells (IT-SOFCs). 2,3 The most extensively studied systems for such applications are \( \text{La}_2\text{Sr}_4\text{NiO}_{6+\delta} \), both experimental (structural and transport) and modelling studies have focused on oxygen overstoichiometric compounds, 4,14 although doping with alkaline-earth atoms on the Ln site can modulate the oxygen content in the system, as well as the average oxidation state of the transition metal ion. 15

Oxygen interstitial migration in \( \text{La}_2\text{NiO}_4 \)-based materials has been shown to be highly anisotropic. 11 This is consistent with computer modelling work 9,11,14 as well as with structural studies based on the maximum entropy method. 5,2 A recent modelling study on the \( \text{La}_2\text{CoO}_{4+\delta} \) compound 14 shows that the oxygen diffusion mechanism is due to a cooperative interstitialcy mechanism, in agreement with that previously proposed for the related \( \text{La}_2\text{NiO}_{4+\delta} \) and \( \text{Pr}_2\text{NiO}_{4+\delta} \) systems. 11

However, heavily acceptor-doped materials and oxygen diffusion via oxygen vacancies have received limited attention; activation energies for oxygen vacancies migration have been calculated for undoped \( \text{La}_2\text{CuO}_4 \) 16 and a recent modelling study on undoped \( \text{La}_2\text{NiO}_4 \) based on energy minimization techniques 13 compares calculated activation energy for vacancy and interstitial migration in this composition.

For the acceptor-doped system \( \text{La}_2\text{Sr}_x\text{CoO}_{4+\delta} \), higher total conductivity has been found for the Sr-rich compositions where the Co oxidation state is close to \( \text{Co}^{3+} \) compared to samples with \( x<1 \). 17,18 This experimental evidence and the suggestion of lower activation energies for oxygen vacancy migration compared to interstitial oxygen in related compounds 13 are aspects which warrant further consideration in view of potential applications of this class of materials.

In this study, we combine energy minimization and molecular dynamics (MD) techniques to investigate, for the first time, the migration paths and energetics for both oxygen vacancy and interstitial mechanisms in the \( \text{La}_2\text{Sr}_x\text{CoO}_{4+\delta} \) system for high Sr levels (\( x > 0.8 \)). Such mechanistic detail is crucial to gain a greater understanding of the transport behavior in \( \text{K}_2\text{NiF}_4 \)-type oxides that underpins their development for next-generation SOFC cathode materials.

2. Methods

In this study, two classes of well established modelling methods have been used, namely static lattice (energy minimization) and molecular dynamics (MD). The GULP code was used for the energy minimization simulations. 19 Interactions between ions were modelled with a Buckingham potential which accounts for electron cloud overlap (Pauli repulsion) and van der Waals interactions. Electronic polarizability was treated using the shell model of Dick and Overhauser. 20 Lattice relaxation around charged defects was treated using the Mott-Littleton method. 21

The short-range potential parameters assigned to each ion-ion interaction were derived by empirical fitting to the observed structural properties, starting from established pair-potential parameters. A mean field approach (partial occupancy on the A
site) using the space group $I4/mmm$ was initially used for the determination of the suitable potential model and the calculation of basic point defects and activation energies for migration.

Calculations were subsequently performed in the $P1$ group where occupancy equal to 1 has been assigned to La and Sr distinct sites, with the lowest energy configuration used for the subsequent defect calculations. Experimental structural parameters for the LaSrCoO$_4$ composition were transferred from our previous work. Details of the potential and shell model parameters used in this study are given in Table S1 (Supplementary Information).

MD simulations were performed with the DL_POLY code using an orthogonal simulation box with periodic boundary conditions. The simulation box consisted of $6 \times 6 \times 4$ unit cells, giving a total of approximately 3000 species in the simulation box; shells were considered for the oxygen atoms only. La and Sr ions, as well as oxygen vacancies and interstitials, were distributed randomly within the simulation box.

Different compositions were reproduced in order to represent both oxygen over-stoichiometric and under-stoichiometric samples. In particular, the following compositions were considered: LaSrCoO$_4$, La$_{0.8}$Sr$_{1.2}$CoO$_{3.9}$, La$_{1.2}$Sr$_{0.8}$CoO$_{4.1}$, La$_{0.8}$Sr$_{1.2}$CoO$_{3.95}$, La$_{1.2}$Sr$_{0.8}$CoO$_{4.05}$. In LaSrCoO$_4$, no defects are present at the beginning of the simulation and the average oxidation state of Co is 3+, in agreement with the experiment. For the La$_{0.8}$Sr$_{1.2}$CoO$_{3.9}$ and La$_{1.2}$Sr$_{0.8}$CoO$_{4.1}$ compositions, a totally ionic compensation (oxygen vacancies or interstitials) of the change in the La/Sr ratio was adopted. For the La$_{0.8}$Sr$_{1.2}$CoO$_{3.95}$ and La$_{1.2}$Sr$_{0.8}$CoO$_{4.05}$ compositions, a partial electronic/ionic compensation of the change in the La/Sr ratio was adopted. In this case, the average Co oxidation state deviates from 3. This last scenario is more representative of the experimental situation. However, since the focus of the present paper is on the mechanistic feature of oxygen transport within this system and, in this respect, we did not notice appreciable differences between the two compensation models proposed, the results presented in the following sections are relative to the totally ionic compensation model. Indeed, for completeness Figures SI-1 and SI-2 show examples of the most frequent migrating events found for the La$_{0.8}$Sr$_{1.2}$CoO$_{3.9}$ and La$_{1.2}$Sr$_{0.8}$CoO$_{4.05}$ compositions, indicating the similarity between the totally ionic and partially electronic compensation models in terms of migration mechanisms.

For the MD simulations, the systems were equilibrated first under a constant pressure of 1 atm and at a specific temperature in the range 1173–1973K for 300,000 time steps (with a time step of 0.5 fs). The average box dimensions derived at each investigated temperature were used during a further equilibration step in the NVT ensemble (Berendsen thermostat) for 60 ps before carrying out the main MD runs of 300 ps. Data analysis was performed using the Visual Molecular Dynamics package (VMD). Such computational techniques have been applied successfully to studies of ion transport in a range of ternary oxides.

### 3. Results and discussion

#### 3.1 Structural modelling and defect sites

LaSrCoO$_4$ crystallizes in the tetragonal space group $I4/mmm$ (S.G. 139). The structure (Figure 1) is composed of CoO$_6$ octahedra connected to form a two-dimensional network by corner-shared oxygen atoms. These layers, similar to those found in the perovskite structure, are separated by (La,Sr)O slabs with the rock-salt structure. Two oxygen crystallographic sites are present within the structure, namely O1 (equatorial position) and O2 (apical position).

First, the potential model succeeded in reproducing the experimental crystal structure, both in the $I4/mmm$ (Table S1) and in the $P1$ (Table S2, Supplementary Information) space groups, within 0.1 Å for the lattice parameters and 0.05 Å for the bond lengths. In particular, the CoO$_6$ octahedral distortion is well reproduced, showing that the elongation of the Co-centred octahedra along the $c$ axis is preserved. The agreement between experimental and calculated structure forms the basis for the subsequent defect calculations.

<table>
<thead>
<tr>
<th>Table 1</th>
<th>Experimental and calculated lattice parameters and bond lengths for LaSrCoO$_4$ in space group $I4/mmm$.</th>
</tr>
</thead>
<tbody>
<tr>
<td>parameter</td>
<td>Exp / Å</td>
</tr>
<tr>
<td>$a$</td>
<td>3.802</td>
</tr>
<tr>
<td>$c$</td>
<td>12.493</td>
</tr>
<tr>
<td>La-O2</td>
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<td>La-O1</td>
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<tr>
<td>Co-O1</td>
<td>1.901</td>
</tr>
<tr>
<td>Co-O2</td>
<td>2.059</td>
</tr>
</tbody>
</table>

Calculations on oxygen defects in the LaSrCoO$_4$ system indicate a preference for the formation of oxygen vacancies in the equatorial plane, localized on the O1 site of the structure. This is in agreement with previous computational results on related phases, such as the La$_2$NiO$_4$ system both in the tetragonal $I4/mmm$ and the orthorhombic system. The most favorable oxygen interstitial position was found to be (0.50 0.00 0.25), as previously proposed for the La$_2$NiO$_4$ system, and close to the experimentally observed position in Pr$_2$NiO$_4$-based mixed phase oxides.
conductors.\textsuperscript{6} Extensive local relaxation occurs around this interstitial position and, as shown in Figure 2, this consists mainly in the partial tilting of the adjacent CoO\textsubscript{6} octahedra to displace the neighbouring O ions. These results are in accord with the anisotropic displacement parameters observed from neutron diffraction studies on related structures.\textsuperscript{6}

Fig. 2 Schematic representation of the local relaxation around the oxygen interstitial defect. Legend - Oxygen interstitial: pink; lattice oxygen: red; Co: green; La/Sr: blue. Grey dotted spheres represent the apical oxygen position before relaxation.

3.2 Oxygen-deficient material: vacancy migration

Several oxygen migration paths and mechanisms have been investigated within the LaSrCoO\textsubscript{4} structure. Static lattice simulations based on energy minimization techniques have been used to calculate the energy profiles for oxygen migration and to derive the activation energy for such processes. These results have been analyzed in view of the scatter plots of atoms positions and the trajectory plots from the MD simulations, in order to elucidate the mechanistic features of oxide ion vacancy migration within this system.

Figure 3 shows schematically the migration paths considered within the unit cell. Oxygen migration via vacancy hopping may proceed through one of the paths labelled from a to e. The energy profiles for the ionic migration involved in each of the migration paths presented in Figure 3 were calculated first considering a linear path between two adjacent equivalent crystallographic positions. Subsequently, possible deviations from the linear path were taken into consideration, allowing the oxygen ion position to relax to the saddle point. This resulted in a curved path characterized by a lower activation energy for migration. Figure 4 shows a comparison between the linear and curved migration energy profiles related to paths b and c (Figure 3), selected as examples. It should be noted that, whereas in Figure 4a (path b of Figure 3) the difference in activation energy between linear and curved paths is relatively high (approximately 1 eV), for Figure 4b (path c of Figure 3) a much smaller difference is found (approximately 0.2 eV).

Table 2 summarizes the calculated activation energies for all the possible migration paths of Figure 3. These data suggest that the lowest migration energy is for path c, which involves vacancy hopping between two adjacent equatorial (O1) positions within the \textit{ab} plane (\textit{i.e.}, the perovskite layer) and along the edge of a CoO\textsubscript{6} octahedron (Figure 3). As found for ABO\textsubscript{3} perovskites such as NdCoO\textsubscript{3},\textsuperscript{26,27} this is predicted to be a slightly curved path where the migrating species is moving away from the central Co ion. Oxygen vacancy migration along paths d (equatorial-apical positions within a CoO\textsubscript{6} octahedron) and a (apical-apical positions involving CoO\textsubscript{6} octahedra in two separate perovskite layers) are also found to be relatively favourable, although with higher migration energies than that found for undoped La\textsubscript{2}NiO\textsubscript{4}.\textsuperscript{13}

Fig. 3 Schematic representation of the oxygen vacancy migration paths in the LaSrCoO\textsubscript{4} structure.

Table 2 Activation energies for oxygen vacancy migration with reference to paths in Figure 3.

<table>
<thead>
<tr>
<th>Migration path</th>
<th>(E_{\text{act}}) (eV)</th>
</tr>
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<tbody>
<tr>
<td>a (O2-O2)</td>
<td>1.26</td>
</tr>
<tr>
<td>b (O2-O2)</td>
<td>2.11</td>
</tr>
<tr>
<td>c (O1-O1)</td>
<td>0.97</td>
</tr>
<tr>
<td>d (O2-O1)</td>
<td>1.14</td>
</tr>
<tr>
<td>e (O1-O1)</td>
<td>6.02</td>
</tr>
</tbody>
</table>

To complement these results and to investigate the mechanistic features of oxide ion vacancy migration in LaSrCoO\textsubscript{4}-based materials in more detail, molecular dynamics (MD) simulations were carried out. Such techniques have proven to be well suited to probe transport mechanisms directly (especially complex correlated ion motion\textsuperscript{28,29}), thus adding to the information derived from the static lattice simulations. Scatter plots of ion coordinates over the simulated time length enable the migration paths to be visualized, and the regions of space most frequently traversed by the different species to be identified. Analysis of the results indicates that oxide ion migration in oxygen-deficient materials proceeds through a vacancy hopping between neighbouring oxygen sites. As expected, no cation diffusion was observed over the simulation time and temperature regime explored.

Figure 5 shows the scatter plot of ion positions from the MD simulation in a perovskite layer. In Figure 5a no vacancy defects were present at the beginning of the simulation (LaSrCoO\textsubscript{4} stoichiometry). In this case, over the simulation time all the ions vibrate around their starting equilibrium positions, as expected. In Figure 5b the data related to the La\textsubscript{0.8}Sr\textsubscript{1.2}CoO\textsubscript{3.9} composition are
presented. The overlapping of colors in Figure 5b indicates that considerable migration has occurred in this layer over the simulation time scale, and that oxide ions originally on crystallographically non-equivalent sites (O1 and O2) have exchanged their positions.

**Fig. 4** Energy profile for oxygen vacancy migration via linear and curved paths in LaSrCoO$_4$: a) apical-apical position (path b of Figure 3); b) equatorial-equatorial position (path c of Figure 3).

Analysis of the scatter plot of ion positions shows that the most frequent transport event is the migration within the $ab$ plane along the edge of CoO$_6$ octahedra between equatorial (O1) positions (equivalent to path c of Figure 3). This is in good agreement with the trend in calculated activation energies presented in Table 2. Long-range migration according to this pathway is highlighted in Figure 5b. This particular event, involving six equatorial oxygen positions, is shown in a 3D representation in Figure 6 where a segment of the CoO$_6$ octahedra is illustrated. Figure 5b also highlights in box Y the curved nature of a vacancy hopping between two equatorial O1 positions (path c of Figure 3). As predicted by energy minimization, the difference in calculated activation energy between linear and curved paths is in this case relatively small (Figure 4b). This helps to rationalise our finding that, over the MD simulation time, the migration path is often visualized also as a straight path.

Other frequent migration events found from the analysis of the MD scatter plots of ion positions are presented in Figure 7, where two adjacent perovskite layers are shown, and indicates vacancy migration associated with paths a and d of Figure 3. In the first case we find oxide-ion migration between two apical positions (O2) belonging to adjacent perovskite layers; in the second case, oxide ion migration involves equatorial (O1) and apical (O2) positions within a CoO$_6$ octahedron.

**Fig. 5** Scatter plot of ion positions from MD simulations viewed down the c axis of a perovskite layer in a) LaSrCoO$_4$ and b) La$_{0.8}$Sr$_{1.2}$CoO$_{3.9}$. Orange, purple and pale blue dots represents ions originally on O1, O2 and Co sites, respectively. La and Sr ions in between layers have been omitted for the sake of clarity.
The trend in the 20.8°C surface energy is consistent with the experimental vacancy migration rates of a different color; spheres of the same color indicate the positions occupied by a specific atom over the simulation time.

Fig. 6 3D representation of the migration event highlighted in box X of Figure 5b, showing long range diffusion involving six equatorial oxygen positions. Each oxygen involved in the migration event is represented by a different color; spheres of the same color indicate the positions occupied by a specific atom over the simulation time.

We note that Figure SI-3 (Supporting Information) shows, as an example, the mean square displacement parameters (MSD) as a function of time for La0.8Sr1.2CoO3.9 at 1773K and indicates that, as predicted, O1 moves faster than O2 while the cations vibrate around their lattice positions. Oxygen diffusion coefficients (D) in the temperature range 1173-1973K were derived from the slope of the mean square displacement parameters (MSD) vs time plots; the mean values of MSD for O1 and O2 have been used since the analysis of the scatter plots and of the MSD vs time plots reveals a simultaneous participation of both species. Calculated oxygen diffusion coefficients are in the range 10^{-5}-10^{-7} cm² s⁻¹ (Figure 8). There are no experimental values for these specific compositions to allow direct comparison, although the calculated range is consistent with the experimental diffusion coefficients derived for the related undoped La2NiO4 and La2CoO4 materials.8,25 The calculated activation energy derived from the MD simulations is 0.57 eV. The trend in the activation energies for oxygen vacancy migration reported in Table 2 is consistent with the results reported for the lanthanum nickelate system,11,13 although the results obtained from MD simulations show a better quantitative agreement.

Fig. 8 Arrhenius plot of the calculated oxygen diffusion coefficient for La0.8Sr1.2CoO3.9.

The experimental indication is that activation energies for oxide ion diffusion in the La2Ni1-xCoxO4+d system decrease as the Co content increases,25 which is reproduced by previous simulation studies of La2NiO4+d and La2CoO4+d,11,12 where the mobile species is interstitial oxygen. We recall here that, in contrast to previous studies, our calculations have been performed on heavily-doped samples in the La2Sr1.5CoO4 system. We therefore calculated the binding energies for the formation of neutral clusters in LaSrCoO4 of configuration [St0La02O]-Sr̅ and La0Sr̅-O̅La0. The estimated binding energies are -0.33 and -0.14 eV/defect, respectively, which suggest that formation of neutral clusters in this system is indeed favoured, and warrant further investigation.

Figure 9 is a 3D representation of the migration paths presented in Figure 7a, where each involved oxygen is indicated with a different color, which clearly show the three migration
paths with lowest activation energies for vacancy migration in the oxygen-deficient LaSrCoO$_4$-based material, as derived by energy minimization techniques (Table 2). In particular, these are (i) vacancy migration between equatorial positions and equatorial-apical positions along the edges of the octahedron, and (ii) vacancy migration between apical positions of CoO$_6$ octahedra belonging to adjacent perovskite layers along the $c$ axis.

Fig. 9 3D representation of the event highlighted in box X of Figure 7a, showing oxygen migration between equatorial and apical positions within a CoO$_6$ octahedron (pink and red), between equatorial and equatorial positions (green) and between apical positions belonging to separate layers (blue). La and Sr ions have been omitted for clarity. Each oxygen involved in the migration event is represented by a different colour; spheres of the same colour indicate the positions occupied by a specific atom over the simulation time.

In summary, analysis of the MD results suggests that oxide ion migration in the $ab$ plane is favoured in oxygen substoichiometric samples, as predicted for undoped La$_2$NiO$_4$ and La$_2$CuO$_4$,[13,16,32] but vacancy migration is not necessarily restricted to the perovskite layer, since jumps do occur between apical oxygens of adjacent layers.

3.3 Oxygen-excess material: interstitial migration

Oxygen interstitial migration in Ni-based K$_2$NiF$_4$-type oxides such as La$_2$NiO$_{4+d}$ has been extensively investigated by modelling techniques, and it has been shown to proceed mainly through an interstitialcy mechanism restricted to the $ab$ plane.[14] The migration path involves the O2 site (apical position) and the oxygen interstitial site.

For completeness, we have also considered the mechanistic details on oxygen interstitial migration in heavily-doped La$_{2+y}$Sr$_x$CoO$_4$ and oxygen-rich materials for the first time. Indeed, the results of this MD study confirm the presence of an analogous migration path and interstitialcy mechanism for the La$_{1.2}$Sr$_0.8$CoO$_{4.1}$ composition.

Figure 10 shows a 3D representation of long-range interstitial migration as derived by MD simulations for La$_{1.2}$Sr$_0.8$CoO$_{4.1}$: the participation of the O2 apical oxygens in the diffusion process is shown, whereas the O1 equatorial positions are not involved.

Fig. 10 3D representation of oxygen interstitial migration in La$_{1.2}$Sr$_0.8$CoO$_{4.1}$. La and Sr ions have been omitted for clarity. Each oxygen involved in the migration event is represented by a different colour. Spheres of the same color indicate the positions occupied by a specific atom over the simulation time.

Oxygen diffusion is therefore highly anisotropic and restricted to the $ab$ plane, in between the perovskite layers. Figure 10 clearly shows the typical “wave-like” migration path observed for interstitial migration in K$_2$NiF$_4$-type oxides from recent modelling studies,[4,11,14] as well from structural studies of Pr$_2$NiO$_4$ based materials using maximum entropy methods.[6,7] Figure SI-2 (supporting information) shows the mean square displacements (MSD) for La$_{1.2}$Sr$_0.8$CoO$_{4.1}$ which confirm that the most mobile species are the O2 apical oxygen and the interstitial oxygen.

For the calculations of the diffusion coefficients, the mean values of MSD for O2 and O3 have been used, since the analysis of the scatter plots and of the MSD vs. time plots reveals a simultaneous participation of both species. The calculated oxygen diffusion coefficients are slightly higher than vacancy diffusion (Figure 11), with a similar activation energy of 0.57 eV.

Fig. 11 Arrhenius plot of the calculated oxygen diffusion coefficient for La$_{1.2}$Sr$_0.8$CoO$_{4.1}$. The line is a guide for the eyes only.

Finally, it is interesting to note that Figure 10 also shows that the migrating oxide-ions have a relatively long residence time at the O2 apical position, and that the region of occupied space around the starting O2 position during the MD simulation is in agreement with the shape and size of the thermal ellipsoids found from neutron diffraction data on related systems.[7] As indicated previously,[14] this accounts for the tilting of the CoO$_6$ octahedra, which assists oxygen migration through the interstitialcy mechanism in this K$_2$NiF$_4$-type structure.
4. Conclusions

A powerful combination of energy minimization and MD techniques has been used to investigate oxide ion migration mechanisms in the heavily doped $K_2NiF_4$-type system, $La_2SrCoO_4$. This class of compounds is receiving considerable attention as potential cathode materials for intermediate temperature solid oxide fuel cells (IT-SOFCs). However, the majority of previous work has focused on oxygen over-stoichiometric samples with no acceptor doping, in which oxide ion migration is mediated only by interstitial oxygen. Here, we present results on the $La_2SrCoO_4$ system with a high level of doping ($x > 0.8$), where both oxygen vacancy and interstitial conduction mechanisms are considered.

Firstly, the results of this study support the hypothesis of favourable migration of oxygen vacancies within the perovskite layer of the structure, but also indicate possible long-range paths between adjacent layers for vacancy conduction; this is of general significance to related acceptor-doped and oxygen-deficient oxides based on $LnSrMO_4$ (where $Ln = La, Nd, Pr; M = Co, Ni, Cu$). Secondly, interstitial oxygen conduction in oxygen hyper-stoichiometric compositions is via an interstitialal mechanism along a 'wave-like' 2D path between apical and interstitial sites within the $ab$ plane, as found for related $K_2NiF_4$ type compounds. Owing to the lack of experimental data on oxygen vacancy diffusion in heavily doped $La_2SrCoO_4$, it is hoped that our study will stimulate further investigations in this area.

Acknowledgement

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Notes and references