A computational and experimental approach linking disorder, high-pressure behaviour and mechanical properties in UiO Frameworks

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Abstract: Whilst many metal organic frameworks possess the chemical stability needed to be used as functional materials, they often lack the physical strength required for industrial applications. Here, we have investigated the mechanical properties of two UiO-topology Zr-MOFs, the planar UiO-67 (Zr6O4(OH)12(bpdc)8, bpdc: 4,4’-biphenyl dicarboxylate) and UiO-abdc (Zr6O4(OH)12(abdc)8, abdc: 4,4’-azobenzene dicarboxylate) via single-crystal nanoindentation, high-pressure X-ray diffraction, density functional theory calculations and first-principles molecular dynamics. On increasing pressure both UiO-67 and UiO-abdc were found to be incompressible when filled with methanol molecules within a diamond anvil cell. Stabilization in both cases is attributed to dynamical linker disorder. The diazo-linker of UiO-abdc possesses local site disorder, which, in conjunction with its longer nature, also decreases the capacity of the framework to compress and stabilizes it against direct compression, compared to UiO-67, characterized by a large elastic modulus. The use of non-linear linkers in the synthesis of UiO-MOFs therefore creates MOFs that have more rigid mechanical properties over a larger pressure range.

Metal-organic frameworks (MOFs) continue to be of exceptional interest to the scientific community because of their guest-specific gas sorption, separation, drug-delivery and catalytic properties.[1] Whilst significant progress has been made in increasing the chemical stability of MOFs,[2] their ‘soft’ mechanical properties often lead to framework collapse or structural distortion upon application of temperature, shear stress or hydrostatic pressure.[3] This poses a severe problem during sintering and pelletization processes, used to shape MOF powders into industrially useful morphologies.[4] Any structural deformation however also alters the highly selective, specific guest-binding properties of MOFs, meaning structural durability is therefore a highly desired quality. Routes to such mechanically robust structures have included embedding MOFs into polymer matrices, or coating nanoparticles with silica,[5] though both lead to substantial deterioration in guest sorption ability.

While sometimes problematic for applications, structural flexibility does however give rise to a very rich and diverse array of pressure- and temperature-induced mechanical responses in MOFs, which may be tuned to individual application needs.[6] The importance of this mechanical behavior motivated us to investigate the link between stimuli-induced mechanical response and chemical structure in the well-known UiO family of Zr-MOFs.

The isoreticular series of UiO-type MOFs consist of Zr6O4(OH)12 nodes, which are interconnected by linear or bent dicarboxylate ligands.[7] The high valency of Zr(IV) and 12-fold coordination of the metal cluster are associated with high shear and bulk moduli, which surpass those of other MOFs.[8] In this work, we build upon recent advances in the synthesis of single crystals of UiO frameworks, and present a combined computational and experimental study of the mechanical behavior

![UiO-67](image)

Figure 1: (a) Synthetic, modulator-based pathway to UiO-67 and UiO-abdc. (b) Unit cell of UiO-67. (c) Unit cell of UiO-abdc (d) enlarged abdc linker. C - grey, O - red, Zr - light blue, N - dark blue, H - omitted for clarity. The scale bar on the crystal photographs represents 100 μm.
of UiO-67 \([\text{Zr}_4\text{O}_4\text{(OH)}_4\text{(bpdca)}_4]\) (bpdca: \(4,4'\text{-biphenyl dicarboxylate}\))\(^{[9]}\) and an azobenzene derivative, UiO-abdc \([\text{Zr}_4\text{O}_4\text{(OH)}_4\text{(abdc)}_4]\) (abdc: \(4,4'\text{-azobenzene dicarboxylate}\))\(^{[9]}\) (Fig. 1). A combination of single-crystal nanoindentation, high-pressure X-ray diffraction studies, density functional theory (DFT) calculations, and first-principles molecular dynamics (MD) simulations are used to show that the dynamic disorder induced in UiO-abdc by the ligand has a significant impact upon the mechanical behavior of the framework.

Synthetic conditions leading to single-crystals of UiO-type MOFs are rare and typically require the addition of a significant excess of monocarboxylic acid crystallization modulators.\(^{[11]}\) We have found the amino acid L-proline to be a highly efficient modulator in the synthesis of Zr UiO-MOFs.\(^{[12]}\) Addition of 5 and 1 equivalents (with respect to the linker) of L-proline and HCl (a known synthetic promoter)\(^{[13]}\) during solvothermal syntheses, yields single crystals of \(\sim 50 \mu\text{m}\) diameter of both UiO-67 and UiO-abdc (SI-1). Both UiO-67 and UiO-abdc crystallize in the cubic space group \(\text{Fm}-3\text{~m} (a = 26.85 \text{ Å} \text{ and } 29.32 \text{ Å} \text{ respectively})\), and contain octahedral cages of diameter 16 Å (UiO-67) and 19 Å (UiO-abdc), which face share with eight smaller tetrahedral pores of diameters 12 Å (UiO-abdc) and 15 Å (UiO-abdc).\(^{[10]}\)

Room temperature single-crystal diffraction data were collected in order to compare to our high-pressure data also collected at room temperature. For UiO-67, some libration is observed on the bpdca ligand, while much larger ellipsoids and more disorder is apparent in the abdc ligand in UiO-abdc. Phenyl rings in UiO-abdc were modelled over three positions (one \(1/2\) occupied, the other \(1/4\) occupied over two positions), while the diazo moiety was modelled over four positions. Both libration and disorder are unsurprising, though the occupational disorder in abdc is ascribed to the lack of ligand mirror symmetry, which the ligand is bisected by via the crystallographic symmetry present. Whilst the average structure is cubic and isostructural with UiO-67, the local structure of the abdc ligand must break this symmetry (Fig. 1d). Interestingly, this disorder did not result in any observable diffuse scattering, which has been a point of great interest recently.\(^{[14]}\)

Quantum mechanical simulations were performed on both UiO-67 and UiO-abdc using the crystallographic coordinates as starting models (SI-2). Motion of the six independent linker arms was followed by MD simulations, which revealed highly dynamic behavior. Atomic probability density functions (PDFs), analogous to thermal ellipsoid models in crystallographic refinements, were derived for the \(\text{Zr}_4\text{O}_4\text{(OH)}_4\) core, and one of the six linker units in each case (Fig. 2).\(^{[15]}\) The resulting plots clearly demonstrate the extent of ligand movement observed across the horizontal mirror plane during the simulations (SI-2). A bowing angle, \(\Theta\), was defined for each ligand (the angle which the benzene carboxylate makes with the Zr metal cluster square plane) and an average magnitude defined for both frameworks. Whilst the bpdca ligands in UiO-67 remain approximately planar (\(<\Theta\> = 3(2)°\)), the geometric frustration in UiO-abdc is accommodated by a more significant bowing of the ligands \(<\Theta\> = 5(3)°\), (Fig. 2). Good agreement between bond distances in the time averaged MD and crystallographic models of both UiO-67 and UiO-abdc (SI-2-Table

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\caption{(a) Top: Mean atomic positions model for UiO-67 (in cyan) superimposed on the crystallographic structure. Bottom: Calculated atomic PDFs, drawn at the standard 50% emphasizing thermal motion in the BPDC linker. (b) Top: Mean atomic positions model for UiO-abdc (in cyan) superimposed on the crystallographically disordered structure. Bottom: Calculated atomic PDFs, drawn at the standard 50% emphasizing thermal motion in the ABDC linker. \(\Theta\) is defined by the intersection of a plane drawn through the equatorial Zr atoms and the carbon atoms of the first aromatic ring on the linker. C – grey, O – red, Zr – light blue, N – dark blue, H – omitted for clarity.}
\end{figure}
1) is observed. The simulated/experimental overlay image of UiO-67 (Fig. 2a) shows close alignment between the MD time-averaged and crystallographic models. In a stark contrast, bowing of the abdc ligand either side of the horizontal mirror plane is clearly observed in UiO-abdc (Fig. 2b).

To investigate the effect of the higher flexibility and geometric frustration of abdc on the mechanical properties of the UiO framework, high-pressure experiments were performed on both UiO-67 and UiO-abdc, by loading suitable single-crystals into modified Merrill–Bassett diamond anvil cells (DAC). In separate experiments, the MOF crystal was then surrounded by either methanol (MeOH) or fluorinated FC-70 as the hydrostatic medium (Fig 3). Pore volume and content as a function of pressure were calculated using the SQUEEZE algorithm within PLATON (SI-4).

On increasing pressure using MeOH as a hydrostatic liquid, both UiO-67 and UiO-abdc expand initially at 0.16 and 0.19 GPa respectively (Fig. 3). Such behaviour has been observed in other compression studies of porous MOFs, where MeOH molecules penetrate into the solid and cause the framework to expand. On increasing pressure further, both frameworks begin to compress, before plateauing at 1.15 and 1.20 GPa in UiO-67 and UiO-abdc, respectively. UiO-67 then remains almost incompressible to 2.4 GPa, while UiO-abdc displays similar behavior to 4.8 GPa. The overall change in unit cell volume of the solvated UiO-abdc of less than 1.2% for such a large pressure regime is highly unusual. Experimental bulk moduli (K) were extracted from the experimental cell volume-pressure relationships using EqS Fit (SI-4). Bulk moduli over a similar pressure range (~0-2 GPa) of 174 GPa and 580 GPa for UiO-67 and UiO-abdc in MeOH were determined from the experimental data, though these numbers cannot be compared to existing literature data due to the over-solvated state of both frameworks. Nevertheless, the drastic change that inclusion of MeOH in the framework pores has on the compressibility is evident from these values, with the more porous MOF with the ‘flexible’ abdc ligand being much more resilient to direct compression on inclusion of MeOH to much higher pressures than observed for the more rigid UiO-67.

On initial pressurization using FC-70 (a mixture of large perfluorinated hydrocarbons, usually considered a non-penetrating hydrostatic medium) indirect evidence of guest inclusion can be observed due to an increase in compressibility observed in UiO-67. On increasing pressure further, direct compression takes place in both frameworks. Unlike with MeOH, further increases in pressure are not accompanied by a plateau in cell volume. In fact, Bragg diffraction is lost from UiO-67 at a relatively modest pressure of 0.3 GPa, yet UiO-abdc undergoes a large change in unit cell volume of almost 10% to 1.8 GPa, while remaining crystalline. Above 1.8 GPa, the quality of data resolution for UiO-abdc was severely reduced, such that structural responses to increasing pressure could not be determined. The ‘flexibility’ of the ligand in UiO-abdc would, however, appear to impart a greater degree of resistance to increasing pressure, whilst remaining crystalline.

In order to determine the compressibility of both frameworks without inclusion of the hydrostatic media, the mean atomic position structures obtained from the MD simulations were geometrically optimized by periodic DFT calculations, and then used as starting models for simulated hydrostatic compression in 0.2 GPa steps up to 1 GPa, thereby simulating direct compression experiments on guest-free frameworks (See SI-3 Fig.3). Compressions in cell volume of ca. 4.0% and 6.0% were observed at 1 GPa, respectively for UiO-67 and UiO-abdc. While a 2nd order Birch–Murnaghan equation of state (SI-4) allowed the determination of a bulk modulus of 16.8 GPa for UiO-abdc, a step in the compression curve for UiO-67 in the 0.2–0.4 GPa range prevents us from making a similar calculation. This hint of a structural transition should be linked to the loss of crystallinity observed experimentally in the same pressure range. These results are similar to previous computational work performed on evacuated MOF-5, which reported ca. 5% compression at 1 GPa and a bulk modulus of 16.52 GPa. Consistent with the mechanical response of MIL-type frameworks, the largest structural responses to the external pressure are observed for the C-O-Zr-Zr angle (φ) of the carboxylate functional group, which undergoes changes of up to 5° during compression of UiO-abdc (SI-3-Fig.3).

For UiO-abdc, the values of bulk moduli calculated from experimental data and calculations are in good agreement, with values of 14 GPa and 16.6 GPa respectively. Because the early onset of pressure amorphization for UiO-67 in FC-70 precludes determination of K, and that value is similarly inaccessible from DFT under compression calculations, we turned to DFT calculations in the elastic regime (with infinitesimal strains). From the elastic tensors obtained (see SI-7), the Voigt-Reuss bulk moduli calculated for UiO-abdc is 15.2 GPa, in good agreement with the data above despite the very different methodology. The bulk modulus of UiO-67 is slightly higher, at 17.4 GPa. Thus, the inclusion of the more flexible azobenzene-based linker logically leads to a softer framework (higher compressibility), though the effect is quantitatively small. In comparison, the effect on the robustness or mechanical stability of the framework is much bigger: a six-fold increase in its hydrostatic pressure at which it loses crystallinity.

In order to look at the response of the material under a different mechanical stimulation, we probed evacuated single crystals of UiO-67 and UiO-abdc by nanoindentation, to determine their Young’s moduli, E, and hardness, H. Single crystal X-ray diffraction was performed to establish Miller indices...
of the crystal facets (SI-5). Using the load-displacement data (SI-6) gained during the indentation, E and H as a function of depth were calculated. The average values for each sample were calculated as \( E = 20.02 \, \text{GPa} \) and \( H = 1.27 \, \text{GPa} \) (UIO-67), and \( E = 13.24 \, \text{GPa} \) and \( H = 0.65 \, \text{GPa} \) (UIO-abdc). The trend seen in Young’s moduli in agreement with values derived from DFT calculations of elastic stiffness tensors, with UIO-abdc again softer than UIO-67 under uniaxial compression (24.1 and 21.5 GPa, respectively).

The elastic modulus of UIO-67 is amongst the largest reported by nanindentation for MOFs, and agrees with the low compressibility of the framework. The magnitude of this rigidity is however surprising, given the empirical inverse relationship observed between \( E \) and framework solvent accessible volume (SAV), which for UIO-67 is only moderately high (65.9%, SI-8).\textsuperscript{[21]} Indeed, HKUST-1 \([\text{Cu}_3(\text{C}_6\text{O}_4\text{H}_2)_2]\) has a similar SAV of 64.3%, yet an elastic modulus of just 9.3 GPa.\textsuperscript{[22]} The framework is also markedly stiffer than the prototypical frameworks ZIF-8 \([\text{Zn(C}_2\text{H}_2\text{N}_2)_2]\) \((E = 3.15 \, \text{GPa})\) and MOF-5 \([\text{ZnO(C}_2\text{H}_4\text{O}_2)_2]\) \((E = 9.5 \, \text{GPa})\), having SAVs of 50.3% and 77.7%, respectively.\textsuperscript{[23]}

The elastic modulus of UIO-abdc is substantially lower than that of UIO-67, which is in agreement with its higher SAV (71.8%). It is interesting to note that this large decrease in rigidity is accompanied by a relatively small increase in SAV, whereas previous work on a different family of MOFs noted that changes in SAV of ca. 20% would be required to elicit decreases in mechanical response of a similar order (ca. 40%).\textsuperscript{[23b]} This vastly more flexible nature is consistent with our observation of the frustrated, bowed nature of the abdc ligand in UIO-abdc.

In conclusion, the different mechanical behavior of two UIO-type frameworks has been fully characterized by computational and experimental methodologies. Bulk and elastic moduli for both UIO-67 and UIO-abdc demonstrate mechanical robustness.\textsuperscript{[24]} The near-zero compressibility of UIO-67 and especially UIO-abdc when over-solvated in MeOH is unique amongst the MOF world, and provides yet another example of the rich physical diversity of these systems, in addition to their much heralded chemical versatility. \( E \) in each case lies above those of other highly porous MOFs, and indeed approach the mechanical response expected of ‘dense’ hybrid frameworks.\textsuperscript{[29]} The large differences in elasticity with relatively small changes in SAV may allow ‘fine-tuning’ of mechanical response in these highly porous systems, though the effect of defects upon the properties of such materials remains an issue.\textsuperscript{[14a, 25]} The unexpected increase in resistance to pressure and the large decrease in the elastic modulus for UIO-abdc compared to UIO-67 are both ascribed to the presence of the azobenzene linker, which bows out of the horizontal plane. Similarly frustrated ‘bowed’ linkers cause significant disorder in other non-UlO MOF structures,\textsuperscript{[27]} and as such may be a general phenomenon which subsequently impacts on their mechanical behavior. These results are important for those looking to introduce flexibility and/or pressure-coping mechanisms in other hybrid MOF systems.

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Entry for the Table of Contents

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Text for Table of Contents

Author(s), Corresponding Author(s)*
Page No. – Page No.
Title

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